

## 2HDMC – a two Higgs Doublet Model Calculator

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We present the program 2HDMC and how it can be used to explore the physics of general CP-conserving two Higgs doublet models.

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## 1. Introduction

Two Higgs doublets models (2HDM) is one of the simplest, non-trivial extensions of the standard model Higgs sector, which appears for example in the Minimal SuperSymmetric Model (MSSM). For a general introduction to 2HDMs and the Higgs sector of MSSM we refer to [1, 2]. A general 2HDM can therefore serve as an effective theory when searching for physics beyond the standard model. In this contribution we describe the program 2HDMC [3] and how it can be used to explore the physics of general CP-conserving 2HDMs <sup>1</sup>.

## 2. General two Higgs doublet models

### 2.1 General two Higgs doublet model potential

We consider the potential for a general model with two complex  $SU(2)_L$  doublets with hypercharge  $Y=1$ :  $\Phi_1, \Phi_2$  which is invariant under global  $SU(2)$  transformations,  $\Phi_a \rightarrow U_{ab}\Phi_b$ , and that is gauge invariant and renormalizable

$$\begin{aligned} \mathcal{V} = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left[ m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.} \right] \\ & + \frac{1}{2} \lambda_1 \left( \Phi_1^\dagger \Phi_1 \right)^2 + \frac{1}{2} \lambda_2 \left( \Phi_2^\dagger \Phi_2 \right)^2 + \lambda_3 \left( \Phi_1^\dagger \Phi_1 \right) \left( \Phi_2^\dagger \Phi_2 \right) + \lambda_4 \left( \Phi_1^\dagger \Phi_2 \right) \left( \Phi_2^\dagger \Phi_1 \right) \\ & + \left\{ \frac{1}{2} \lambda_5 \left( \Phi_1^\dagger \Phi_2 \right)^2 + \left[ \lambda_6 \left( \Phi_1^\dagger \Phi_1 \right) + \lambda_7 \left( \Phi_2^\dagger \Phi_2 \right) \right] \left( \Phi_1^\dagger \Phi_2 \right) + \text{h.c.} \right\} \end{aligned}$$

Demanding that the potential is real implies that  $m_{11}^2, m_{22}^2, \lambda_{1-4}$  are real whereas  $m_{12}^2, \lambda_{5-7}$  in general can be complex. However, if we demand that there is no explicit CP-violation then the latter parameters also have to be real.

### 2.2 Electroweak symmetry breaking

As usual the electroweak symmetry is broken by non-zero vacuum expectation values (vev) of  $\Phi_1$  and/or  $\Phi_2$ . After applying the minimization conditions of the potential the  $m_{11}^2$  and  $m_{22}^2$  parameters can be traded for the vev's of the two doublets:  $v_1 = v \cos \beta$  and  $v_2 = v e^{i\xi} \sin \beta$  with  $v = (\sqrt{2}G_F)^{-1/2} \approx 246$  GeV. Here  $\xi$  is a possible phase that we put to zero by demanding that there is no spontaneous CP-violation. The two doublets can then be written as

$$\begin{aligned} \Phi_1 &= \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2} (G^+ \cos \beta - H^+ \sin \beta) \\ v \cos \beta - h \sin \alpha + H \cos \alpha + i (G^0 \cos \beta - A \sin \beta) \end{pmatrix} \\ \Phi_2 &= \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2} (G^+ \sin \beta + H^+ \cos \beta) \\ v \sin \beta + h \cos \alpha + H \sin \alpha + i (G^0 \sin \beta + A \cos \beta) \end{pmatrix} \end{aligned}$$

where  $G^+$  and  $G^0$  are the Nambu-Goldstone bosons that give masses to the  $W$  and  $Z$  bosons respectively,  $H^+$  is the charged Higgs boson,  $A$  is a CP-odd and  $h, H$  are CP-even neutral Higgs bosons (with  $m_h \leq m_H$ ), and  $\tan \beta$  defines a basis in  $\Phi$  space. (Also note that there is a special basis, the

<sup>1</sup>Admittedly, given the format for these proceedings, this description will have to be quite limited and incomplete and we apologize for that. For a more complete description we refer to [3] and references therein.

Higgs basis, where only one of the fields develops a vev and therefore  $\tan\beta = 0$  or  $\cot\beta = 0$ ). With these conventions the couplings of Higgs and electroweak gauge bosons are given by the invariant  $s_{\beta-\alpha} \equiv \sin(\beta - \alpha)$  and  $c_{\beta-\alpha} \equiv \cos(\beta - \alpha)$ . Finally we note that in addition to the above parameterisation of the potential it can also be useful to use the masses of the Higgs bosons as parameters. Thus in the 2HDMC program the user can choose between the so called general parameterisation,  $\{m_{12}^2, \lambda_{1-7}, \tan\beta\}$  or the physical one  $\{m_{12}^2, m_h, m_H, m_A, m_{H^\pm}, s_{\beta-\alpha}, \lambda_{6-7}, \tan\beta\}$  in addition to the Higgs basis which is the same as the general one but with  $\tan\beta = 0$  and  $m_{H^\pm}$  replacing  $m_{12}^2$ . For backward compatibility the program can also handle the basis used in the Higgs Hunter's Guide [1]. It is important to note that the program uses conventions where  $\tan\beta \geq 0$  and  $s_{\beta-\alpha} \geq 0$ .

### 2.3 Possible additional symmetries

In addition to the symmetries already discussed it is also possible to impose other interesting symmetries on the potential. First we note that one can demand an additional  $U(1)_{PQ}$  (Peccei-Quinn) symmetry [4] by setting  $m_{12}^2 = 0$  and  $\lambda_{5-7} = 0$ . The discrete version of this symmetry is to demand an exact  $Z_2$  symmetry such that the potential is symmetric under  $\Phi_1 \rightarrow \Phi_1, \Phi_2 \rightarrow -\Phi_2$  which leads to  $m_{12}^2 = 0$  and  $\lambda_{6-7} = 0$ . This symmetry is softly broken if  $m_{12}^2 \neq 0$ , which leads to flavour changing neutral currents beyond tree-level. Finally in the case of a supersymmetric theory the potential takes a special form which at tree-level leads to

$$\lambda_1 = \lambda_2 = \frac{g^2 + g'^2}{4}, \quad \lambda_3 = \frac{g^2 - g'^2}{4}, \quad \lambda_4 = -\frac{g^2}{2}, \quad \lambda_5 = \lambda_6 = \lambda_7 = 0, \quad m_{12}^2 = m_A^2 \cos\beta \sin\beta.$$

For convenience the program contains two special methods for setting up: a tree-level MSSM model with parameters  $m_A$  and  $\tan\beta$ , as well as a so called inert doublet (ID) model [5] with  $\{m_h^{\text{SM}}, m_H^{\text{ID}}, m_A^{\text{ID}}, m_{H^\pm}^{\text{ID}}, \lambda_2, \lambda_3\}$  as parameters.

### 3. Theoretical constraints

The 2HDMC program also contains methods for checking theoretical constraints on the parameters describing the potential, namely positivity, perturbativity and tree-level unitarity.

Demanding that the potential is bounded from below one has the constraints [7] :  $\lambda_1 > 0$ ,  $\lambda_2 > 0$ ,  $\lambda_3 > -\sqrt{\lambda_1\lambda_2}$ . In addition, in the case  $\lambda_6 = \lambda_7 = 0$  one has  $\lambda_3 + \lambda_4 - |\lambda_5| > -\sqrt{\lambda_1\lambda_2}$  whereas if  $\lambda_6, \lambda_7 \neq 0$  one gets  $\lambda_3 + \lambda_4 - \lambda_5 > -\sqrt{\lambda_1\lambda_2}$  as well as more complicated constraints which take too much room to include here, but are included in the program.

The constraints from perturbativity are obtained by considering the cross-sections for  $2 \rightarrow 2$  Higgs scattering processes, which can be written as a perturbative series in the square of the corresponding quartic couplings  $\lambda_{H_i H_j H_k H_l}^2 / (16\pi^2)$ . In order for this series to make sense the couplings cannot be too large and the program contains a method for checking this with the default limit being  $\lambda_{H_i H_j H_k H_l} < 4\pi$ .

A similar constraint on the parameters of the Higgs potential is obtained by requiring tree-level unitarity [8] for  $HH$  and  $HV_L$  scattering (with  $V_L$  denoting the longitudinal parts of  $W$  or  $Z$ ), which

corresponds to putting limits on the eigenvalues  $\Lambda_{(Y,\Sigma)}$  of the following scattering matrices

$$\begin{aligned}
16\pi S_{(2,1)} &= \begin{pmatrix} \lambda_1 & \lambda_5 & \sqrt{2}\lambda_6 \\ \lambda_5 & \lambda_2 & \sqrt{2}\lambda_7 \\ \sqrt{2}\lambda_6 & \sqrt{2}\lambda_7 & \lambda_3 + \lambda_4 \end{pmatrix} \\
16\pi S_{(2,0)} &= \lambda_3 - \lambda_4 \\
16\pi S_{(0,1)} &= \begin{pmatrix} \lambda_1 & \lambda_4 & \lambda_6 & \lambda_6 \\ \lambda_4 & \lambda_2 & \lambda_7 & \lambda_7 \\ \lambda_6 & \lambda_7 & \lambda_3 & \lambda_5 \\ \lambda_6 & \lambda_7 & \lambda_5 & \lambda_3 \end{pmatrix} \\
16\pi S_{(0,0)} &= \begin{pmatrix} 3\lambda_1 & 2\lambda_3 + \lambda_4 & 3\lambda_6 & 3\lambda_6 \\ 2\lambda_3 + \lambda_4 & 3\lambda_2 & 3\lambda_7 & 3\lambda_7 \\ 3\lambda_6 & 3\lambda_7 & \lambda_3 + 2\lambda_4 & 3\lambda_5 \\ 3\lambda_6 & 3\lambda_7 & 3\lambda_5 & \lambda_3 + 2\lambda_4 \end{pmatrix}
\end{aligned}$$

The default value for the limit is  $|\Lambda_{(Y,\Sigma)}| < 16\pi$ .

#### 4. Yukawa sector

The program contains a general Yukawa sector parameterized in terms of the matrices  $\rho^L$ ,  $\rho^D$ , and  $\rho^U$  in flavour space for leptons, down-type, and up-type quarks respectively:

$$\begin{aligned}
-\mathcal{L}_Y &= \bar{D} \frac{\kappa^D s_{\beta-\alpha} + \rho^D c_{\beta-\alpha}}{\sqrt{2}} Dh + \bar{D} \frac{\kappa^D c_{\beta-\alpha} - \rho^D s_{\beta-\alpha}}{\sqrt{2}} DH + i\bar{D}\gamma_5 \frac{\rho^D}{\sqrt{2}} DA \\
&+ \bar{U} \frac{\kappa^U s_{\beta-\alpha} + \rho^U c_{\beta-\alpha}}{\sqrt{2}} Uh + \bar{U} \frac{\kappa^U c_{\beta-\alpha} - \rho^U s_{\beta-\alpha}}{\sqrt{2}} UH - i\bar{U}\gamma_5 \frac{\rho^U}{\sqrt{2}} UA \\
&+ \bar{L} \frac{\kappa^L s_{\beta-\alpha} + \rho^L c_{\beta-\alpha}}{\sqrt{2}} Lh + \bar{L} \frac{\kappa^L c_{\beta-\alpha} - \rho^L s_{\beta-\alpha}}{\sqrt{2}} LH + i\bar{L}\gamma_5 \frac{\rho^L}{\sqrt{2}} LA \\
&+ [\bar{U}\{V_{CKM}\rho^D P_R - \rho^U V_{CKM} P_L\} DH^+ + \bar{\nu}\rho^L P_R LH^+ + \text{h.c.}]
\end{aligned}$$

where  $P_{R/L} = (1 \pm \gamma_5)/2$  and  $\kappa^F \equiv \sqrt{2}M^F/v$  are diagonal matrices determined by the fermion masses. The only constraint on  $\rho^F$  is that they are symmetric.

Models with non-diagonal  $\rho^F$  will lead to non-minimal flavour violating charged currents as wells as flavour changing neutral currents. This can be avoided [6] by imposing a  $Z_2$  symmetry on  $\Phi_1$ ,  $\Phi_2$  and  $U_R$ ,  $D_R$ ,  $L_R$  such that each fermion type only couples to one Higgs doublet. In turn this leads to the restriction  $\rho^F = \kappa^F \cot \beta$  or  $\rho^F = -\kappa^F \tan \beta$ , which means that there are four different types of  $Z_2$  symmetric 2HDMs. For simplicity the program also contains methods for specifying the Yukawa sector by simply choosing the type.

#### 5. Partial decay widths

With both the Higgs sector and the Yukawa sector being specified the program can then be used to calculate partial decay widths and branching ratios for range of processes including:

- $H \rightarrow ff'$  with optional (N)LO QCD corrections
- $H \rightarrow gg$  with optional LO QCD corrections
- $H \rightarrow HH$
- $H \rightarrow HV^*$  including off-shell vector bosons
- $H \rightarrow VV^*$  including off-shell vector bosons
- $H \rightarrow \gamma\gamma$
- $t \rightarrow H^+b$

where  $H = \{h, H, A, H^\pm\}$  denotes any applicable Higgs boson and  $V = \{Z, W\}$ .

## 6. Experimental constraints

Before using the program to make predictions in a specific model one may also want to take into account existing experimental constraints. This is not a simple task and there are dedicated programs for this. Therefore, the program has been limited to having methods for calculating the 2HDM contribution to the oblique parameters [9]:  $S, T, U, V, W, X$  compared to the SM with Higgs mass  $m_h^{\text{ref}}$ , as well as the contribution to the muon anomalous magnetic moment. In order to take into account collider and flavour limits the program contains interfaces to HiggsBounds (version 2) [10] and SuperIso [11] respectively.

## 7. Usage/parameter-setting/input-output

The 2HDMC program has been written in a modular fashion with an object oriented structure using C++. It can either be used in library mode where the different methods are called by the user program or as “ready to compile” command line type programs which are distributed together with the main code.

The code, manual, and full class documentation can be downloaded from <http://www.isv.uu.se/thepp/MC/2HDMC>. In order to compile the program one needs a gcc compiler (3.4 and 4 tested) and the GNU Scientific Library (GSL) installed. There is a template makefile which should be adapted to the local conditions and there is a test program Demo with which the successful installation can be tested.

The code consist of four main classes

- **SM**: to give the Standard Model input parameters with running  $\alpha_s$  and quark masses
- **THDM**: to specify a general two-Higgs doublet model in terms of the Higgs and Yukawa sectors
- **Constraints**: to calculate theoretical and experimental constraints on the 2HDM
- **DecayTable**: to calculate the decay modes of 2HDM Higgs bosons and the top quark

For a more complete description we refer to the class documentation which can be found on the 2HDMC homepage.

In order to simplify the communication with other programs there is also a LesHouches style input/output format and one can also export a given 2HDM as a user model for MadGraph/MadEvent [12] to calculate cross-sections etc.

## 8. Summary and conclusions

The 2HDMC program is a versatile and flexible program for exploring the physics of general CP-conserving 2HDMs: all the way from defining the model and checking it against theoretical and experimental constraints, to exploring its phenomenology such as calculating decay widths and scattering cross-sections. Some examples of its use can be found in [13, 14, 15, 16].

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